

Exercises to the lecture  
Algorithmic Automata Theory  
Sheet 1

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Delivery until 23.04.2019 at 15:00

**Exercise 1.1** (Languages and Formulas)

- a) Find a WMSO-formula  $\varphi$  such that  $L(\varphi) = \Sigma^* a \Sigma^* b^+$ .
- b) What is the language described by  $\exists y \forall x \forall z: (x < y \wedge y < z) \rightarrow \neg P_a(x) \wedge P_b(y)$  ?

**Exercise 1.2** (WMSO to Finite Automata)

Using the method presented in the lecture, construct a finite automaton that accepts the language defined by the formula

$$\varphi = \exists x \exists y: x < y \wedge P_a(x) \wedge P_a(y) .$$

**Exercise 1.3** (WMSO Expressiveness)

- a) Show that  $\text{WMSO}[<, \text{suc}]$  and  $\text{WMSO}[\text{suc}]$  are equally expressive.
- b) Show that  $\text{WMSO}[<, \text{suc}]$  and  $\text{WMSO}[<]$  are equally expressive.

Delivery until 23.04.2019 at 15:00 into the box next to 343 or in the class