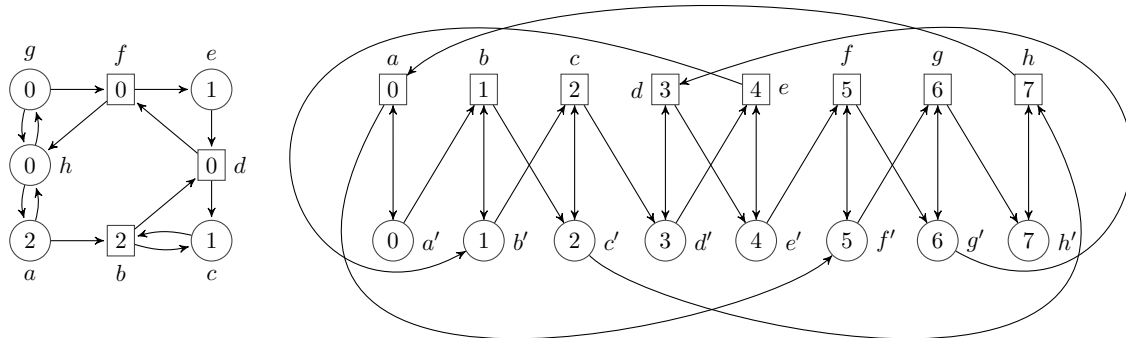


## Exercise Sheet 12

### Exercise 12.1 Parity Game Determinacy

Use the McNZSolver procedure from class to solve the parity games from last week:



### Exercise 12.2 Parity Tree Automata

Let  $\Sigma = \{a/2, b/2, c/2\}$ . Give Parity Tree Automata for each of the languages below:

- (a)  $L_1 = \{t \in \mathcal{T}_\Sigma^\omega \mid t = a(b(t, t), b(t, t))\}$ ,
- (b)  $L_2 = \{t \in \mathcal{T}_\Sigma^\omega \mid t(\epsilon) = a \text{ and } \forall x : t(x) = a \Rightarrow t(x110) = a \wedge t(x001) = a\}$ ,
- (c)  $L_3 = \{t \in \mathcal{T}_\Sigma^\omega \mid \text{for every path } \sigma \text{ of } t : \infty\text{-many } a\text{'s on } \sigma \Rightarrow \infty\text{-many } b\text{'s on } \sigma\}$ ,
- (d)  $L_4 = \{t \in \mathcal{T}_\Sigma^\omega \mid \text{there are finitely many } a\text{'s on every path of } t\}$ .

Which of the above languages are recognised by deterministic Parity Tree Automata?

*Note: deterministic PTAs are strictly less powerful than nondeterministic PTAs.*