

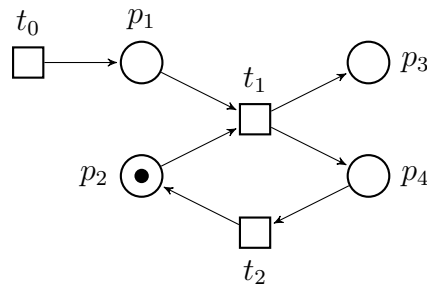
Exercise Sheet 7

Problem 1: Complements of downward-closed sets

Let (Q, \leq) be a qo and $B \subseteq Q$. Show that $\overline{B \downarrow}$ is upward-closed.

Problem 2: Backwards search for Petri nets

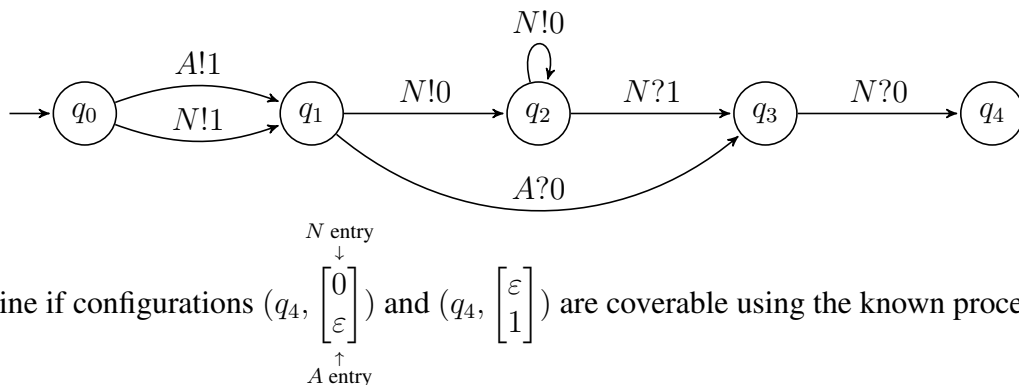
- a) Give an algorithm to compute minpre for Petri nets. Argue about its correctness.
- b) Consider the following Petri net:



Run the backwards search to prove that the marking $M = (0 \ 0 \ 2 \ 0)$ is coverable.

Problem 3: Backwards search for LCS

Consider the LCS depicted in the figure below.



Determine if configurations $(q_4, \begin{bmatrix} 0 \\ \varepsilon \end{bmatrix})$ and $(q_4, \begin{bmatrix} \varepsilon \\ 1 \end{bmatrix})$ are coverable using the known procedure.

Problem 4: Reduction of Boundedness

We call a LCS *bounded* if its configuration space is finite.

Reduce boundedness of reset nets to boundedness of LCS, i.e. given a reset net R , construct a LCS S_R such that R is bounded iff S_R is bounded. Argue correctness of the construction.